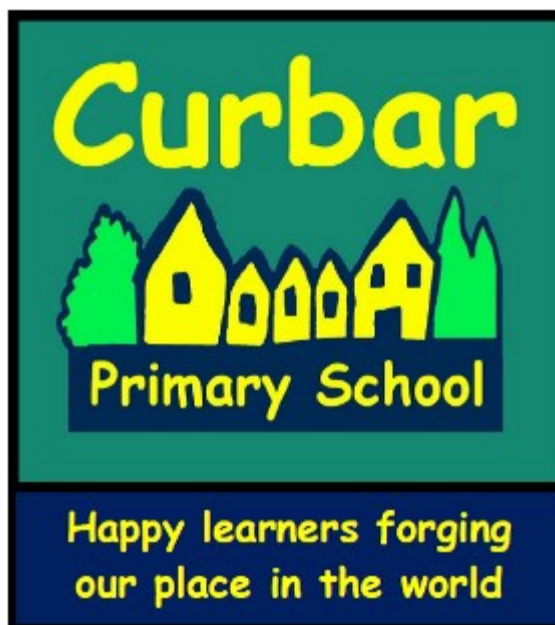


Curbar Primary School

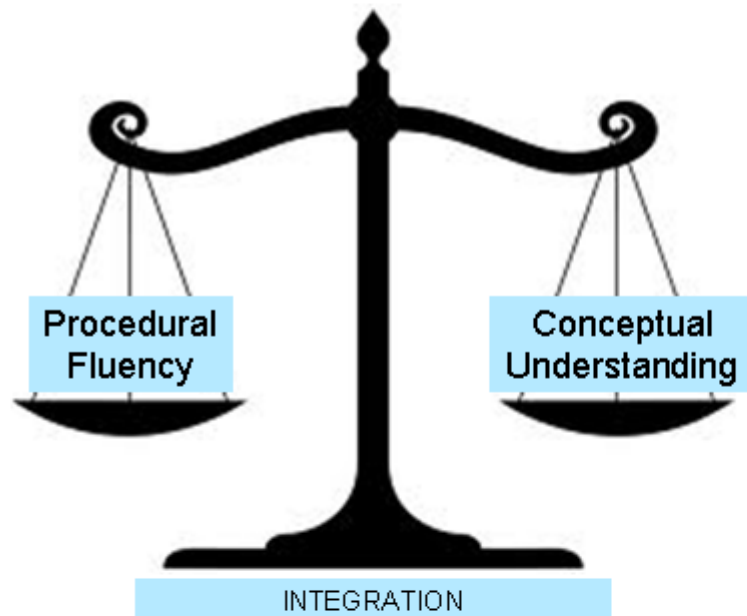
Calculation Policy

(Jan 2023)

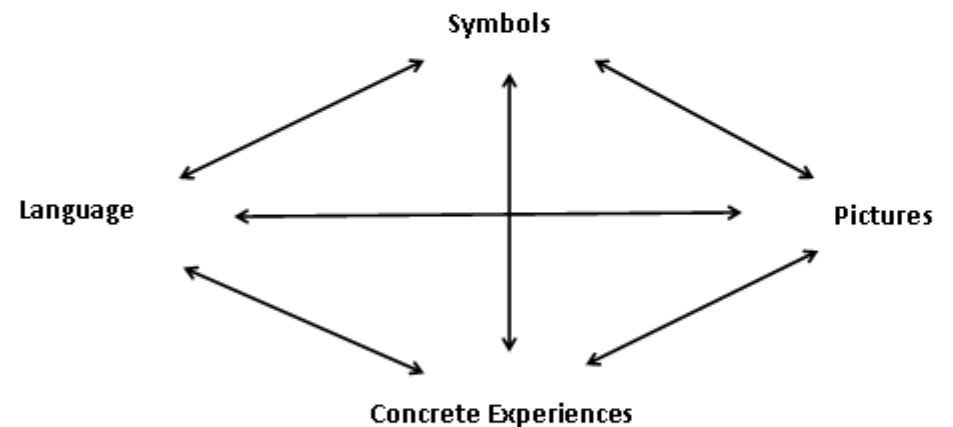


Aims:

Developing procedural fluency and conceptual understanding in parallel, through using concrete, pictorial and symbolic representations and making connection between them.


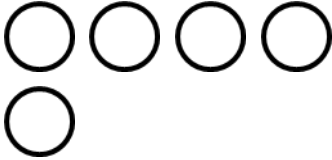



Haylock and Cockburn (2008)





Addition and Subtraction

EYFS Calculations Policy Development Matters Band: 22-36 Months			
Addition	Subtraction	Multiplication	Division
Objectives: Selects a small number of objects from a group when asked, for example, 'please give me one', 'please give me two'. Recites some number names in order. Uses some language of quantities, such as 'more' and 'a lot'. Begins to make comparisons between quantities. Creates and experiments with symbols and marks representing ideas of numbers. Knows that a group of things change in quantity when something is added or taken away.			
Vocabulary: Number names, count, number, forwards, more, add, lots, some, altogether	Vocabulary: Take away, backwards, less, left	Vocabulary:	Vocabulary:
Use of role play and environment. Practical activities using addition Songs and rhymes.  Practical activities as above but beginning to use number tracks as models to support understanding.	Number rhymes and songs with actions. Use of practical resources to illustrate the song E.g. 5 currant buns in the bakers shop..... And took it right away  		

Objectives:

- Uses some number names and number language spontaneously.
- Uses some number names accurately in play.
- Recites numbers in order to 10.
- Knows that numbers identify how many objects are in a set.
- Beginning to represent numbers using fingers, marks on paper or pictures.
- Sometimes matches numeral and quantity correctly.
- Shows curiosity about numbers by offering comments or asking questions.
- Compares two groups of objects, saying when they have the same number.
- Shows an interest in number problems.
- Separates a group of three or four objects in different ways, beginning to recognise that the total is still the same.
- Shows an interest in numerals in the environment.
- Shows an interest in representing numbers.
- Realises not only objects, but anything can be counted, including steps, claps or jumps.

Vocabulary: Number names to 10, add, How many, lots, some, most, add, more, forwards, count

Vocabulary: Take away, backwards, least, less, left

Recognise numbers 1- 10

0 1 2 3 4 5 6 7 8 9 10

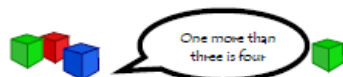


Spot numbers in the environment

Count up to 10 objects reliably



Conservation



Find one more than a number

Recording numbers using pictures or use apparatus, such as Numicon to show this.



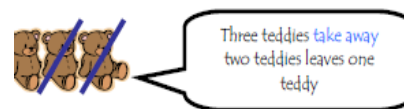
Continue to count back in ones from any given number


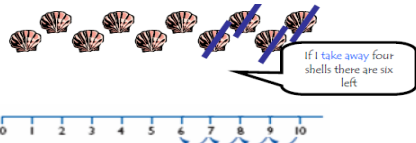
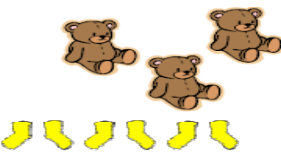
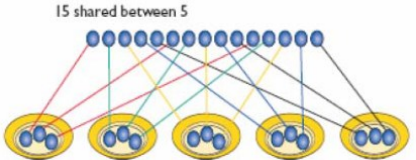
10, 9, 8, 7, ...

Remove some objects and count

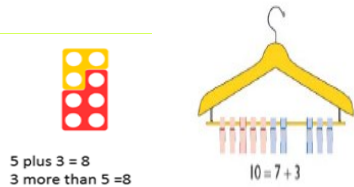
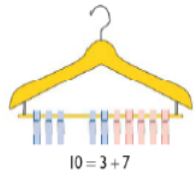


Begin to relate subtraction to taking away



EYFS Calculations Policy	Development Matters Band: 40-60 months and ELG		
Addition	Subtraction	Multiplication	Division
<p>Objectives: Recognise some numerals of personal significance.</p> <ul style="list-style-type: none"> • Recognises numerals 1 to 5. • Counts up to three or four objects by saying one number name for each item. • Counts actions or objects which cannot be moved. • Counts objects to 10, and beginning to count beyond 10. • Counts out up to six objects from a larger group. • Selects the correct numeral to represent 1 to 5, then 1 to 10 objects. • Counts an irregular arrangement of up to ten objects. • Estimates how many objects they can see and checks by counting them. • Uses the language of 'more' and 'fewer' to compare two sets of objects. • Finds the total number of items in two groups by counting all of them. • Says the number that is one more than a given number. • Finds one more or one less from a group of up to five objects, then ten objects. • In practical activities and discussion, beginning to use the vocabulary involved in adding and subtracting. • Records, using marks that they can interpret and explain. • Begins to identify own mathematical problems based on own interests and fascinations. <p>Early Learning Goal Children count reliably with numbers from one to 20, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer.</p>		<p>Objectives: Early Learning Goal They solve problems, including doubling, halving and sharing.</p>	
<p>Vocabulary: More than, enough, count on, lots of, bigger, most, addition, add on, plus, forwards, before, total, higher, up</p>	<p>Vocabulary: Less than, fewer, least, enough, count back, smaller, take away, difference, before, down, backwards, lower</p>	<p>Vocabulary: Double, lots of, groups, equal</p>	<p>Vocabulary: Share, halve, groups of</p>
<p>Begin to relate addition to combining groups of numbers</p>  <p>Demonstrate their knowledge of addition by combining Numicon shapes and say what they have done using the appropriate vocabulary.</p>	<p>Count backwards along a number line to 'take away'</p>  <p>Use Numicon to support subtraction. Place a small piece over a larger piece to see what is left and visualise the connection between addition and subtraction.</p>	<p>Role play/small world / story telling etc, find pairs of.</p> <p>e.g. How many socks will we need for the three bears?</p>  <p>Experience of equal groups of objects, count in 2s, 5s and 10s. Work on practical problem solving activities involving equal sets or groups.</p>	<p>Sorting objects into groups e.g. We have got 4 biscuits how can we share them out equally (fairly) between the two of us?</p> 

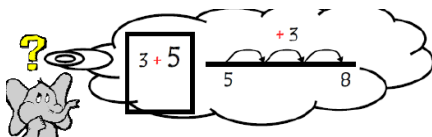
Start to recognise that addition can be done in any order



Use Numicon to help with number facts



Put the biggest number first and count on

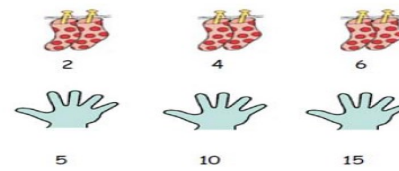


Begin to use the + and = signs to record calculations in a number sentence using practical apparatus for support.

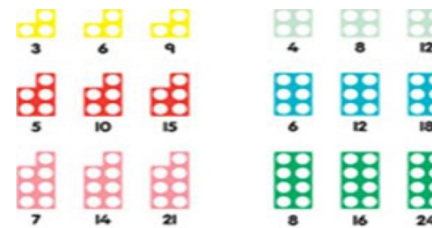
$$8 + 7 = 15$$

Begin to use the – and = signs to record calculations in a number sentence, using practical apparatus for support.

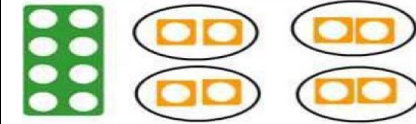
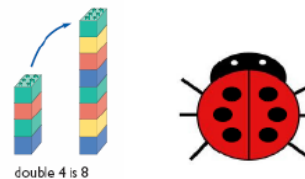
$$6 - 4 = 2$$



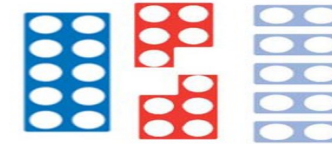
Use Numicon to help the children to visualise the grouping of numbers and to support counting on as repeated addition.



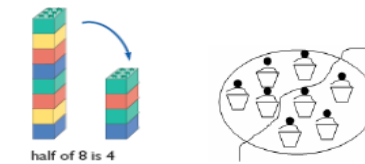
Know number doubles to 10



Numicon used to find how many smaller numicon pieces fit over a larger piece. e.g. 5, 2's will fit over a 10 piece.



Know number halves to 10



Addition



Year 1

Objectives: add and subtract one digit and two digit numbers within 20, including 0. Use the + and - signs.

Vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line

Subtraction



To put the biggest number first and count on.
To add two single digit numbers that bridge 10.

- Count along a number line to add numbers together



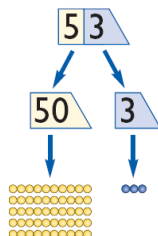
To begin to partition numbers in different ways e.g.,

$$50 = 40 + 10$$

Record as a number sentence both linear and columnar

E.g. $10 = 7 + 3$

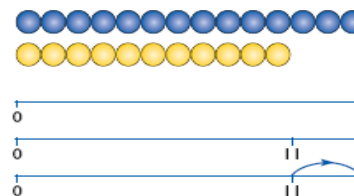
$$7 + 3 = 10$$



To subtract single digit numbers often bridging



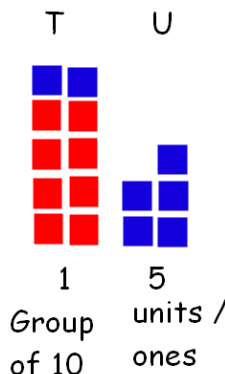
Begin to find the difference by counting up from the smallest number.



The difference between 11 and 14 is 3.
 $14 - 11 = 3$
 $11 + \square = 14$

My End of Year Method

$8 + 7 = 15$



Methods for both addition and subtraction mirror a practical process. The written method should represent a practical procedure and record the steps taken to remove value. E.g. $15 - 7 = 8$; 15 balls (arranged as 10 and 5) where 5 is removed and recorded, then 2 is removed and the remaining 8 regrouped into the ten

My End of Year Method

$15 - 7 = 8$

Addition



Year 2

Objectives: add and subtract two 2 digit numbers and three 1 digit numbers. Add and subtract a two digit number and ones and a two digit number and tens. Show that addition can be done in any order and subtraction of one number from another cannot. Recognise and use the inverse relationship between addition and subtraction.

Vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, **sum, tens, units, partition, addition, column, tens boundary**

Subtraction

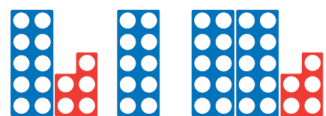
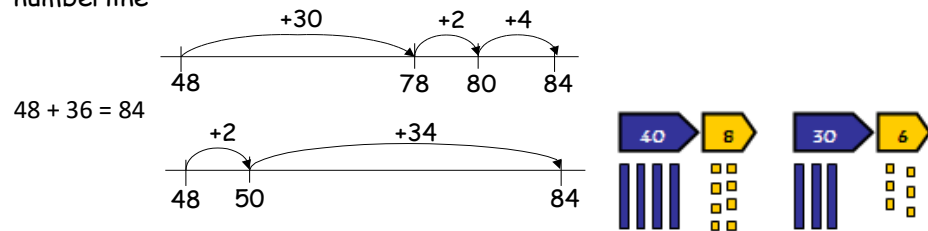


Horizontal addition two digit and single digit number

$$24 + 8 = 32$$



To add two 2 digit numbers (bridging through the tens boundary) using a numberline

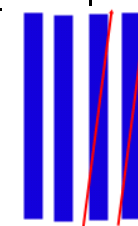


$$15 + 10 = 25$$

$$\begin{aligned} 48 + 36 &= 84 \\ 40 + 30 &= 70 \\ 8 + 6 &= 14 \\ 70 + 14 &= 84 \end{aligned}$$

Partition the number to be subtracted
No regrouping

$$\begin{aligned} 43 - 20 &= 23 \\ 23 - 3 &= 20 \end{aligned}$$



2 Groups of 10
0 ones/units

My End of Year Method

These methods should be taught alongside each other. The written procedure should reflect practical fluency

My End of Year Method

$$\begin{aligned} 43 - 20 &= 23 \\ 23 - 3 &= 20 \end{aligned}$$

Addition



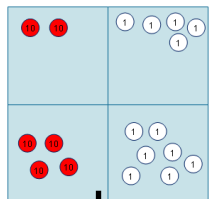
Year 3

Subtrac-

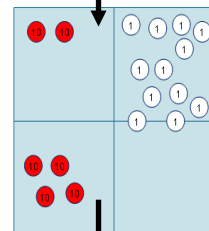


Objective: Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

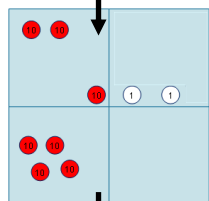
vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, **hundreds boundary, increase, vertical, exchanging, expanded, compact**



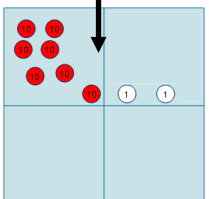
$$\begin{array}{r} 25 \\ +47 \\ \hline \end{array}$$



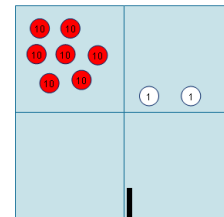
$$\begin{array}{r} 25 \\ +47 \\ \hline \end{array}$$



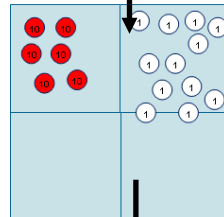
$$\begin{array}{r} 25 \\ +47 \\ \hline 2 \end{array}$$



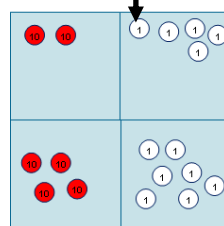
$$\begin{array}{r} 25 \\ +47 \\ \hline 72 \end{array}$$



$$\begin{array}{r} 72 \\ -47 \\ \hline \end{array}$$



$$\begin{array}{r} 72 \\ -47 \\ \hline \end{array}$$



$$\begin{array}{r} 72 \\ -47 \\ \hline 25 \end{array}$$

End of Year Method

789 + 642 becomes

$$\begin{array}{r} 789 \\ +642 \\ \hline 1431 \\ \hline 11 \end{array}$$

End of Year Method

<p>874 - 523 becomes</p> $\begin{array}{r} 874 \\ -523 \\ \hline 351 \end{array}$	<p>932 - 457 becomes</p> $\begin{array}{r} 932 \\ -457 \\ \hline 475 \end{array}$
---	---

Children will also become familiar with the bar model and part-whole model to aid in the visual representation of addition and subtraction.

Addition



Year 4

Subtrac-



Objective: add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate

Vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, vertical, **exchanging**, expanded, compact, **thousands, hundreds, digits, inverse**

Children to continue to use resources and grids to support calculation.

(*See Year 3)

End of Year Method

$$\begin{array}{r} 3517 \\ + 396 \\ \hline 3913 \end{array}$$

End of Year Method

$$\begin{array}{r} 2754 \\ - 1562 \\ \hline 1192 \end{array}$$

Addition



Year 5

Objectives: Add and subtract whole numbers with more than 4 digits

Vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, vertical, **exchanging**, expanded, compact, vertical, thousands, hundreds, digits, inverse and **decimal places, decimal point, tenths, hundredths, thousandths**

Subtraction



$$\begin{array}{r}
 \text{£ } 23.59 \\
 + \text{£ } 7.55 \\
 \hline
 \text{£ } 31.14
 \end{array}$$

Numbers should exceed 4 digits

Decimal point should stay aligned throughout

Compact column subtraction with 'exchanging'

$$\begin{array}{r}
 \overset{2}{\cancel{3}} \overset{10}{\cancel{1}} \overset{10}{0} \overset{4}{\cancel{5}} \overset{16}{6} \\
 - \quad \quad 2128 \\
 \hline
 28928
 \end{array}$$

Multi-step word problems in contexts

Rounding to check answers

My End of Year Method

$$\begin{array}{r}
 23,481 \\
 + \quad 1,362 \\
 \hline
 24,843
 \end{array}$$

My End of Year Method

$$\begin{array}{r}
 \overset{6}{\cancel{7}} \overset{10}{\cancel{1}} \overset{16}{6} \overset{9}{\cancel{9}} \cdot \overset{10}{0} \\
 - \quad \quad 372.5 \\
 \hline
 6796.5
 \end{array}$$

Addition



Subtraction



Year 6
Objectives: Add and subtract whole numbers with more than 4 digits
Vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, vertical, ex-changing , expanded, compact, vertical, thousands, hundreds, digits, inverse and decimal places, decimal point, tenths, hundredths, thousandths

	2	3	.	3	6	1
		9	.	0	8	⊙
	5	9	.	7	7	⊙
+		1	.	3	⊙	⊙
<hr/>						
	9	3	.	5	1	1
	2	1		2		

Numbers should exceed 4 digits

Decimal point should stay aligned throughout

Compact column subtraction with 'exchanging'

	7	10	'5	.	4	'1	9	kg
-		3	6	.	0	8	⊙	kg
<hr/>								
		6	9	.	3	3	9	kg

Multi-step word problems in contexts

Estimating and rounding to check answers

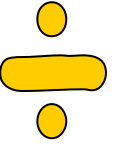
Insert zeros into empty columns

My End of Year Method

	8	1	,	0	5	9	
		3	,	6	6	8	
		1	,	5	3	0	1
+	2	0	,	5	5	1	
<hr/>							
	1	2	,	0	5	7	9
		1		1	1	1	

My End of Year Method

	7	10	,	6	9	9	
-		8	,	9	4	9	
<hr/>							
		6	,	0	7	5	0



Multiplication and Division

Multiplication

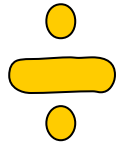


Year 1

Objectives: solve one step problems involving multiplication and division by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. Count in 2,5 and 10s.

Vocabulary: groups of, lots of, times, array, altogether, multiply, count

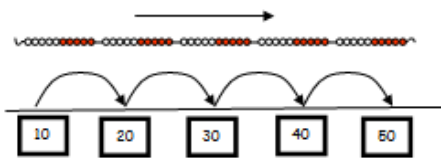
Division



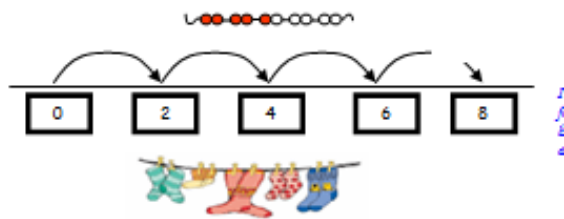
How many legs will 3 teddies have?



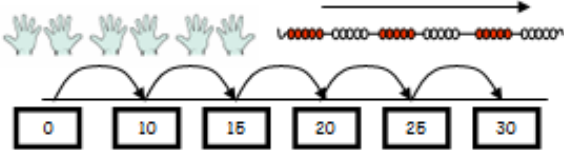
Count on in tens



Count in twos from zero



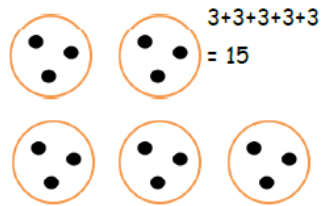
Count in 5s from zero



$4 \times 3 =$ 4 multiplied by 3 = $4 + 4 + 4$

$3 \times 4 =$ 3 multiplied by 4 = $3 + 3 + 3 + 3$

There are 3 sweets in one bag. How many sweets are in 5 bags altogether?

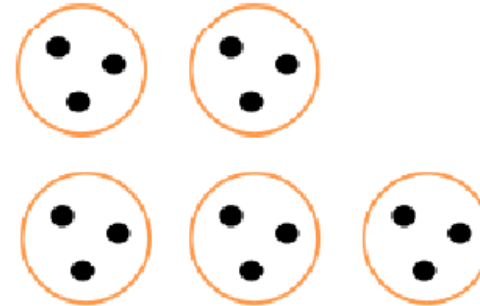


Division mat—sharing.

A group of objects shared equally between a predetermined set of groups.

Some children may be able to record as and solve from:

$15 \div 5 = 3$



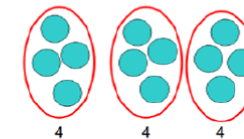
- Trough role play/general play situations find pairs of. e.g. How many socks will we need for the three bears?
- Sorting objects into groups e.g. We have got 4 biscuits how can we share them out equally (fairly) between the two of us?
- Playing pairs game i.e. snap, pairs

How many groups of 4 can be made with 12 stars? = 3

Grouping:



Sharing:



12 shared between 3 is 4

Example division problem in a familiar context:

There are 6 pupils on this table and there are 18 pieces of fruit to share between us. If we share them equally, how many will we each get?

Can they work it out and give a division statement...?

"18 shared between 6 people gives you 3 each."

Multiplication

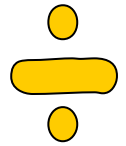


Year 2

Objectives: recall and use multiplication and division facts for the 2,5 and 10 multiplication tables, calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication, division and equals symbols, solve problem involving multiplication and division using materials, arrays, repeated addition, mental methods, multiplication and division facts.. Count in 3,4 and 8s.

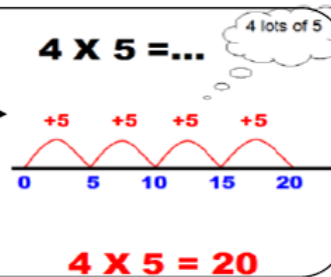
Vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, **repeated addition, column, row, commutative, sets of, equal groups, times as big as, once, twice, three times...**

Division

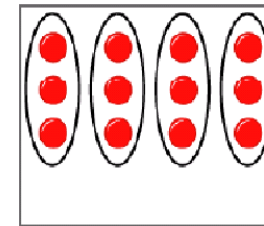


Use repeated addition on a number line:

- Starting from zero, make equal jumps up on a number line to work out multiplication facts and write multiplication statements using x and = signs.



Arrays:



This represents $12 \div 4 = 3$
 12 counters shared equally into 4 groups
 Pupils should also know that 12 counters shared into groups of 4 will produce 3 groups of 4 counters.

Use arrays:



$5 \times 3 = 15$

$5 \times 3 = 3 + 3 + 3 + 3 = 15$

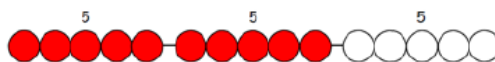
$3 \times 5 = 5 + 5 + 5 = 15$

$3 \times 5 = 15$

Use arrays to help teach children to understand the commutative law of multiplication, and give examples such as $3 \times \underline{\quad} = 6$.

Use practical apparatus:

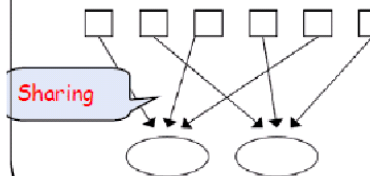
$5 \times 3 = 5 + 5 + 5$



Know and understand sharing and grouping:

6 sweets shared between 2 people, how many do they each get?

Grouping



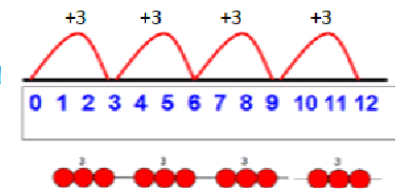
There are 6 sweets, how many people can have 2 sweets each?



Children should be taught to recognise whether problems require sharing or grouping.

Grouping using a number line:

Group from zero in equal jumps of the divisor to find out 'how many groups of $\underline{\quad}$ in $\underline{\quad}$?. Pupils could and using a bead string or practical apparatus to work out problems like 'A CD costs £3. How many CDs can I buy with £12?' This is an important method to develop understanding of division as grouping.



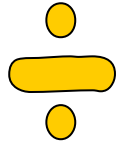
$12 \text{ divided by } ? = 3$

Multiplication



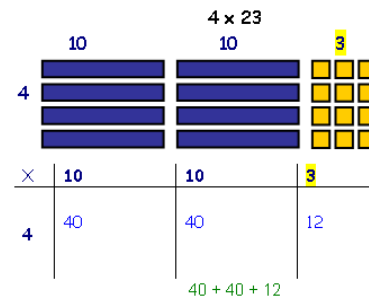
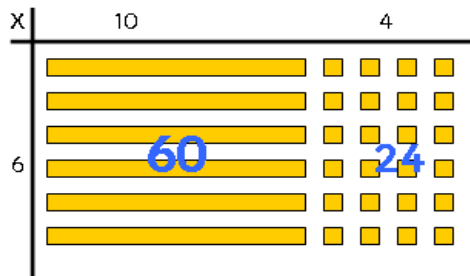
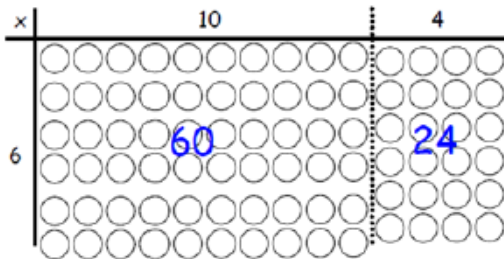
Year 3

Division



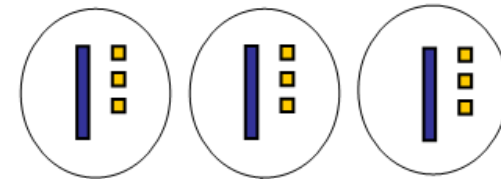
Objective: Write and calculate mathematical statements for multiplication and division using the multiplication tables they know, including for two-digit numbers times one digit numbers, using mental and progressing to formal written methods.

Vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative, sets of, equal groups, times, times as big as, once, twice, three times..., **partition, grid method, multiple, product, tens, units, value exchanging**

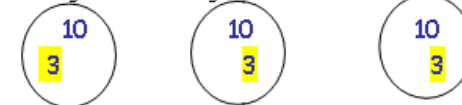


- Using chunking as an efficient way of sharing (using place value apparatus to share)

eg $39 \div 3 = 13$



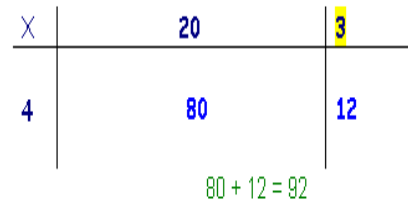
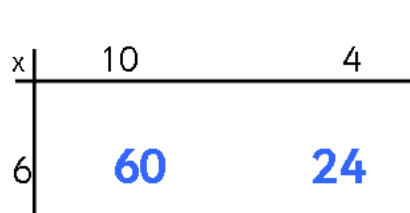
- Chunking numbers together to share



- Begin to chunk in larger chunks on a number line



End of Year Method



End of Year Method



Sharing $39 \div 3 =$
 $30 \div 3 = 10$
 $9 \div 3 = 3$ $10 + 3 = 13$

Multiplication



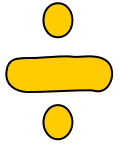
Year 4

Objective: Multiply two and three digit numbers by a one digit number using formal written layout.

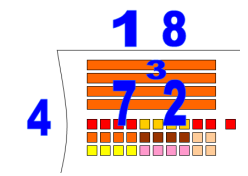
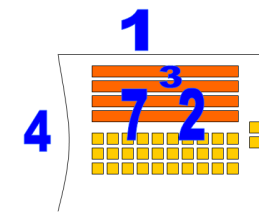
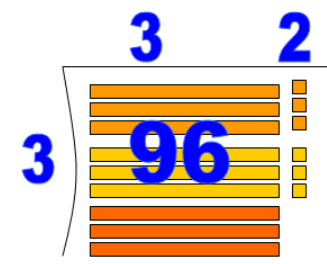
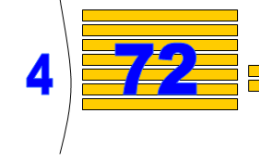
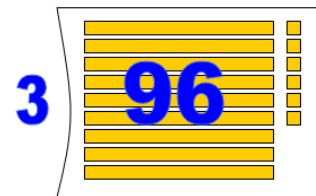
Pupils practice to become fluent in the formal written method of short multiplication and for multiplying an short division with exact answers when dividing by a 1 digit number.

Vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, array, column, row, commutative, groups of, sets of, lots of, equal groups, times, multiply, times as big as, once, twice, three times... partition, grid method, total, multiple, product, sets of, **inverse exchanging**

Division



$$\begin{array}{r}
 x \quad 10 \qquad \qquad 4 \\
 \hline
 6 \quad 60 \qquad \quad 24
 \end{array}$$



End of Year Method

$$\begin{array}{r}
 14 \\
 \times 6 \\
 \hline
 24 \\
 60 \\
 \hline
 84
 \end{array}$$

End of Year Method

$$\begin{array}{r}
 32 \\
 3 \overline{) 96} \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 18 \\
 4 \overline{) 72} \\
 \hline
 \end{array}$$

Multiplication



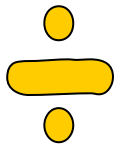
Year 5

Objectives: Multiply up to 4-digits by 1 or 2 digits.

Divide up to 4 digits by a single digit, including those with remainders.

Vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, array, column, row, commutative, sets of, equal groups, times as big as, once, twice, three times... partition, grid method, total, multiple, product, inverse, **square, factor, integer, decimal,**

Division



$$\begin{array}{r}
 24 \\
 \times 16 \\
 \hline
 144 \\
 240 \\
 \hline
 384
 \end{array}$$

Multi-step word problems in contexts

Estimating and rounding to check answers

Interpret remainders in context

$$\begin{array}{r}
 27 \\
 36 \overline{) 972} \\
 \underline{- 720} \\
 252 \\
 \underline{- 252} \\
 0
 \end{array}$$

20x
 7x
 Answer : 27

My End of Year Method

$$\begin{array}{r}
 12 \\
 124 \\
 \times 26 \\
 \hline
 744 \\
 2480 \\
 \hline
 3224 \\
 11
 \end{array}$$

My End of Year Method—
Short

$$\begin{array}{r}
 146 \\
 35 \overline{) 5110} \\
 \underline{1621} \\
 1621
 \end{array}$$

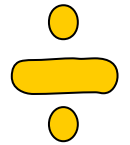
My End of Year Method—
Long

$$\begin{array}{r}
 28 \\
 15 \overline{) 432} \\
 \underline{300} \quad 15 \times 20 \\
 132 \\
 \underline{120} \quad 15 \times 8 \\
 12
 \end{array}$$

~~15~~ = $\frac{1}{5}$



Year 6



Objectives: Multiply decimals with up to 2d.p by a single digit.

Divide at least 4 digits by both single-digit and 2-digit numbers

Vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated ad-dition, array, column, row, commutative, sets of, equal groups, times as big as, once, twice, three times... partition, grid method, total, multiple, product, inverse, square, factor, integer, decimal, short / long multiplication, **tenths, hundredths, decimal** exchanging

$$\begin{array}{r}
 24 \\
 \times 16 \\
 \hline
 144 \\
 240 \\
 \hline
 384
 \end{array}$$

3	.	1	9
\times	8		
<hr/>			
2	5	.	5
	1		7

Multi-step word problems in contexts

Estimating and rounding to check answers Interpret remainders in context

Children working at greater depth will experience multiplication and division problems involving decimals.

$$\begin{array}{r}
 27 \\
 36 \overline{) 972} \\
 \underline{- 720} \\
 252 \\
 \underline{- 252} \\
 0
 \end{array}$$

20x
 7x
 Answer : 27

My End of Year Method

$$\begin{array}{r}
 12 \\
 124 \\
 \times 26 \\
 \hline
 744 \\
 2480 \\
 \hline
 3224 \\
 11
 \end{array}$$

My End of Year Method— Short

$$\begin{array}{r}
 14.6 \\
 35 \overline{) 511.0} \\
 \underline{1621} \\
 5110
 \end{array}$$

My End of Year Method— Long

$$\begin{array}{r}
 28 \\
 15 \overline{) 432} \\
 \underline{300} \quad 15 \times 20 \\
 132 \\
 \underline{120} \quad 15 \times 8 \\
 12
 \end{array}$$

$\frac{432}{15} = \frac{4}{5}$